## Physics 831 Quiz #5 - Friday, Oct. 11

- 1. A molecule, which lives in a **one-dimensional** world, has mass m and two internal states: a ground state and a single excited state which is at energy X above the ground state. Initially, a low-density gas of such molecules is at temperature  $T_i$  before expanding and cooling isentropically to a temperature  $T_f$ .
  - (a) (5 pts) What is the initial energy per particle? Give answer in terms of m,  $T_i$ , X and the initial density per unit length  $\rho_i$ .
  - (b) (10 pts) Derive an expression for the initial entropy per particle in terms of the same variables. Begin with the expression,

$$S = \ln Z + \beta E$$
,

where

$$Z = \frac{z^N}{N!},$$

$$z = z_{\text{int}} \frac{L}{2\pi\hbar} \int dp \ e^{-p^2/2mT}.$$

(c) (5 pts) After insentropically cooling to  $T_f$ , find the density  $\rho_f$ . Give answer in terms of  $\rho_i$ ,  $T_i$ ,  $T_f$  and X.

Fun facts to know and tell:  $\lim_{N\to\infty} \ln(N!) = N \ln N - N$