1. A drop of poison is placed into the middle of a long narrow pipe carrying water. The poison then diffuses away from the initial position, x = 0, toward  $x = \pm \infty$ . The diffusion equation is

$$\frac{\partial \rho}{\partial t} = D \frac{\partial^2 \rho}{\partial x^2}$$

where  $\rho$  is the number of poison molecules per unit length. If the net number of molecules is N, find an expression for  $\rho(x, t)$  in terms of N and D.

2. Consider a non-accelerating Hubble expansion, where freezeout occurs for both photons and the mythical spartino at a temperature of  $T_0 = 3 \times 10^5$  K, when the age of the universe is  $\tau_0 = 1.4 \times 10^5$  years. The phase space density of the photons at this time is thermal with temperature  $T_0$ . The spartino is an extremely massive fermionic particle, whose phase space density at freeze-out was also thermal and was given by:

$$f_{\text{spartino}}(p,\tau_0) = \frac{\exp\left(\mu_0/T_0 - p^2/2mT_0\right)}{1 + \exp\left(\mu_0/T_0 - p^2/2mT_0\right)}.$$

Later, at a time  $\tau$ , the spartino's phase distribution is

$$f_{\text{spartino}}(p,\tau) = \frac{\exp\left(\mu/T - p^2/2mT\right)}{1 + \exp\left(\mu/T - p^2/2mT\right)}$$

For time  $\tau = 1.4 \times 10^{10}$  years, find

- (a) The temperature describing the spectrum of photons.
- (b) The temperature T describing the spartino spectrum above
- (c) In terms of  $\mu_0$ , what is the new chemical potential  $\mu$ ?