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Physics 321 Exercise: Differential Scattering October 30, 2023

1. A neutron is incident on a target where it experiences a potential energy:

$$
V(r)=\left\{\begin{array}{rr}
V_{0}, & r<R \\
0, & r>R
\end{array}\right.
$$

(a) (5 pts) If $V_{0}=+\infty$, what is the total cross section?
(b) (3 pts) If $V_{0}$ is positive, but finite, the cross section is

- bigger.
- smaller.
- the same.
(c) $(2 \mathrm{pts})$ If $V_{0}$ is negative, but finite, the cross section is
- bigger.
- smaller.
- the same.

2. You are an experimentalist and you have measured counts in your detector. The beam was neutrons scattering off a lead target. The mass density of lead is $11.29 \mathrm{gm} / \mathrm{cm}^{3}$ and the mass of a lead atom is $3.44 \times 10^{-22} \mathrm{~g}$. The thickness of the target is 0.5 microns. You have 90 detector elements set at scattering angles of $2,4,6, \cdots, 180$ degrees. Each detector's cross sectional area is a 1 cm by 1 cm square, and is positioned 0.75 m from the target. A beam is aimed at the target, with $5 \times 10^{12}$ neutrons impinging the target over the course of the experiment. Your detector elements have perfect efficiency and record the number of counts in the table below.
(a) ( 5 pts ) What is the angular coverage, $d \Omega$, of each detector element?
(b) ( 5 pts ) Calculate and plot $d \sigma / d \Omega$ in barns as a function of $\theta$. ( 1 barn $\left.=10^{-24} \mathrm{~cm}^{2}\right)$.

| $\theta_{s}(\mathrm{deg})$ | counts |  |  |
| ---: | :--- | ---: | :--- |
| 2.0 | 442730 |  |  |
| 4.0 | 438673 | 92.0 | 1864 |
| 6.0 | 431988 | 94.0 | 2187 |
| 8.0 | 422786 | 96.0 | 2476 |
| 10.0 | 411222 | 98.0 | 2724 |
| 12.0 | 397483 | 100.0 | 2927 |
| 14.0 | 381791 | 102.0 | 3084 |
| 16.0 | 364394 | 104.0 | 3196 |
| 18.0 | 345558 | 106.0 | 3266 |
| 20.0 | 325566 | 108.0 | 3296 |
| 22.0 | 304704 | 110.0 | 3290 |
| 24.0 | 283262 | 112.0 | 3253 |
| 26.0 | 261520 | 114.0 | 3189 |
| 28.0 | 239752 | 116.0 | 3102 |
| 30.0 | 218211 | 118.0 | 2997 |
| 32.0 | 197130 | 120.0 | 2877 |
| 34.0 | 176719 | 122.0 | 2747 |
| 36.0 | 157159 | 124.0 | 2610 |
| 38.0 | 138604 | 126.0 | 2469 |
| 40.0 | 121176 | 128.0 | 2326 |
| 42.0 | 104968 | 130.0 | 2184 |
| 44.0 | 90045 | 132.0 | 2044 |
| 46.0 | 76441 | 134.0 | 1908 |
| 48.0 | 64168 | 136.0 | 1778 |
| 50.0 | 53212 | 138.0 | 1653 |
| 52.0 | 43540 | 140.0 | 1535 |
| 54.0 | 35099 | 142.0 | 1424 |
| 56.0 | 27825 | 144.0 | 1321 |
| 58.0 | 21639 | 146.0 | 1225 |
| 60.0 | 16457 | 148.0 | 1137 |
| 62.0 | 12187 | 150.0 | 1056 |
| 64.0 | 8736 | 152.0 | 982 |
| 66.0 | 6010 | 154.0 | 915 |
| 68.0 | 3916 | 156.0 | 854 |
| 70.0 | 2366 | 158.0 | 800 |
| 72.0 | 1275 | 160.0 | 752 |
| 74.0 | 565 | 162.0 | 710 |
| 76.0 | 164 | 164.0 | 673 |
| 78.0 | 8 | 166.0 | 641 |
| 80.0 | 40 | 168.0 | 614 |
| 82.0 | 209 | 170.0 | 591 |
| 84.0 | 474 | 172.0 | 573 |
| 86.0 | 799 | 174.0 | 559 |
| 88.0 | 1153 | 176.0 | 550 |
| 90.0 | 1514 | 178.0 | 544 |
| 180.0 | 542 |  |  |
|  |  |  |  |

