

your name(s) _____

Physics 851 Exercise #1 - Monday, Sept. 13th

Work in groups of 3 (assigned in class) to complete this assignment. You can use the following link to get some templates (with some of these steps already completed)

<https://people.nslc.msu.edu/pratt/phy851>

Templates can be found at the bottom of the web page. C++ users will have to install EIGEN3 package.

Using either C++ or python, write a program to create and manipulate the following 3×3 matrix,

$$H = \begin{pmatrix} 1 & 2i & 3 \\ -2i & 2 & -2i \\ 3 & 2i & 3 \end{pmatrix}.$$

1. On your laptop, create the matrix H , then find its inverse. Multiply them together and print the product, showing that its unity.
2. Find the eigenvalues and eigenvectors. Print out the eigenvectors as a matrix, and print out the eigenvector with the lowest eigenvalue.
3. Demonstrate that for each eigenvector, v_ℓ , that $Hv_\ell = \lambda_\ell v_\ell$.
4. Show that if the matrix of eigenvalues is called U^\dagger , with each column representing an eigenvector, that the matrix UHU^\dagger is diagonalized with the eigenvalues found above.
5. Choose a constant B so that the lowest eigenvalue of $H - B$ has an absolute value larger than the absolute value of any other eigenvalue of $H - B$. Then take a vector v with all its elements set to unity. Then write a loop where you contract $H - B$ and v to get a new vector v ,

$$v = (H - B)v,$$

then normalize v and repeat n times. Demonstrate that for large n you reproduce the eigenvector of H with the lowest eigenvalue, i.e. the ground state wave function if H is a Hamiltonian.