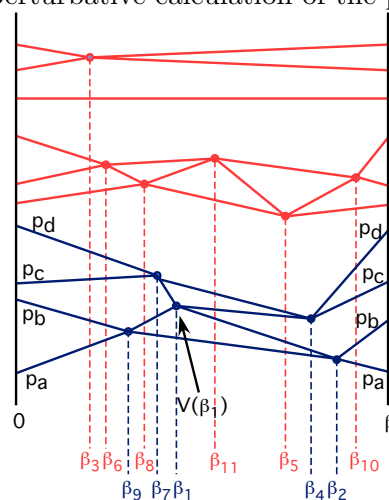


YOUR NAME: _____

1. The diagram represents a perturbative calculation of the partition function.



Consider the connected diagram involving $p_a \rightarrow p_d$ which when used to calculate the pressure contributes at order n in perturbation theory and to order m in powers of $e^{\beta\mu}$, i.e., the prefactor is $e^{m\beta\mu}$. Circle one of the below:

| | | |
|-----------------|-----------------|------------------|
| $n = 4, m = 4$ | $n = 4, m = 5$ | $n = 4, m = 12$ |
| $n = 5, m = 4$ | $n = 5, m = 5$ | $n = 5, m = 12$ |
| $n = 12, m = 4$ | $n = 12, m = 5$ | $n = 12, m = 12$ |

none of the above

2. Consider a virial expansion for a non-relativistic two-dimensional gas of spin-zero bosons of mass m at temperature T ,

$$\frac{P}{\rho T} = 1 + \sum_{m=2}^{\infty} A_m \left(\frac{\rho}{\rho_0} \right)^{m-1}, \quad \rho_0 \equiv \frac{mT}{2\pi\hbar^2}.$$

Ignoring interactions between the particles, calculate A_2 .

3. Consider two states:

$$|\alpha\rangle = e^{\alpha a^\dagger} |0\rangle, \quad |\beta\rangle = e^{\beta a^\dagger} |0\rangle.$$

Find the overlap, $\langle\alpha|\beta\rangle$.